## Adjacency matrix

 8 Implementation


Arfan Shahzad

| Data Structures and Algorithms |
| :--- |
| Course Contents: |
| Abstract data types, complexity analysis, Big Oh notation, Stacks (linked lists and |
| array implementations), Recursion and analyzing recursive algorithms, divide and |
| conquer algorithms, Sorting algorithms (selection, insertion, merge, quick, bubble, |
| heap, shell, radix, bucket), queue, dequeuer, priority queues (linked and array |
| implementations of queues), linked list \& its various types, sorted linked list, searching |
| an unsorted array, binary search for sorted arrays, hashing and indexing, open |
| addressing and chaining, trees and tree traversals, binary search trees, heaps, M-way |
| tress, balanced trees, graphs, breadth-first and depth-first traversal, topological order, |
| shortest path, adjacency matrix and adjacency list implementations, memory |
| management and garbage collection |

## Adjacency Matrix and adjacency list implementation

- An adjacency matrix is a 2D array (matrix) that represents the edges between vertices in a graph.
- The rows and columns of the matrix represent the vertices, and the values in the matrix represent the edges.


## Adjacency Matrix and adjacency list implementation cont...

- If there is an edge between vertices $i$ and $j$, then the value in the matrix at the i -th row and j -th column (or j -th row and i -th column, depending on the graph being directed or undirected) will be 1.
- Otherwise, the value will be 0 .
- Here's an example of an adjacency matrix for an undirected graph with 4 vertices:


## Adjacency Matrix and adjacency list implementation cont...

|  | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 0 | 1 | 0 | 1 |
| 2 | 1 | 0 | 1 | 1 |
| 3 | 0 | 1 | 0 | 0 |
| 4 | 1 | 1 | 0 | 0 |

## Adjacency Matrix and adjacency list implementation cont...

- An adjacency list is a data structure that represents a graph as a collection of lists, where each list represents the vertices adjacent to a particular vertex.
- Each vertex is assigned a list of its adjacent vertices.
- If there is an edge between vertices $i$ and $j$, then vertex $i$ will have $j$ in its list, and vertex $j$ will have $i$ in its list.


## Adjacency Matrix and adjacency list implementation cont...

- If the graph is directed, then only the out-neighbors are included in the list for each vertex.
- Here's an example of an adjacency list for the same undirected graph as above:


## Adjacency Matrix and adjacency list implementation cont...

$$
\begin{aligned}
& 1: 2,4 \\
& 2: 1,3,4 \\
& 3: 2 \\
& 4: 1,2
\end{aligned}
$$

## Adjacency Matrix and adjacency list implementation cont...

- In this example, vertex 1 is adjacent to vertices 2 and 4 , vertex 2 is adjacent to vertices 1,3 , and 4 , vertex 3 is adjacent to vertex 2 , and vertex 4 is adjacent to vertices 1 and 2 .

